

COMPETITIVE ENTRANCE

2015 SESSION

Department: Civil Engineering and Forestry Techniques, Electrical and Power Engineering, Mechanical Engineering and Computer Science
1st Cycle Option ALL

Paper 2: Mathematics

Duration 3hrs

1. The partial fraction decomposition form of $\frac{2x^2-1}{x^2(x-1)}$ is

a) $a + \frac{b}{x} + \frac{c}{x^2} + \frac{d}{x-1}$
 b) $a + \frac{b}{x} + \frac{c}{x^2} + \frac{d}{x-1}$
 c) $\frac{bx+c}{x^2} + \frac{d}{x-1}$ d) $\frac{ax+b}{x^2} + \frac{c}{x-1}$

La décomposition en éléments simple $\frac{2x^2-1}{x^2(x-1)}$ est

b) $a + \frac{b}{x} + \frac{c}{x^2} + \frac{d}{x-1}$
 b) $a + \frac{b}{x} + \frac{c}{x^2} + \frac{d}{x-1}$
 c) $\frac{bx+c}{x^2} + \frac{d}{x-1}$ d) $\frac{ax+b}{x^2} + \frac{c}{x-1}$

2. The coefficient of the term in x^0 in the binomial expansion of $\left(2x - \frac{1}{x^2}\right)^6$ is

a) 240 b) 480 c) 180 d) 20

Les coefficients des termes en x^0 du développement de $\left(2x - \frac{1}{x^2}\right)^6$ est

b) 240 b) 480 c) 180 d) 20

3. The smallest positive value of x which satisfy the equation $\cos\left(x + \frac{\pi}{12}\right) = \frac{1}{2}$ is

a) $\frac{\pi}{3}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{6}$ d) $\frac{5\pi}{12}$

La plus petite valeur de x qui satisfait l'équation $\cos\left(x + \frac{\pi}{12}\right) = \frac{1}{2}$ est :

b) $\frac{\pi}{3}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{6}$ d) $\frac{5\pi}{12}$

4. The complex number $Z = -1 + i$ satisfies $\frac{z+1}{z+2-i} = a + i$. The value of a is:

a) -1 b) 1 c) 0 d) 2

le nombre complexe $Z = -1 + i$ satisfait $\frac{z+1}{z+2-i} = a + i$. La valeur de a est.

a) -1 b) 1 c) 0 d) 2

5. The coordinates of the turning point on the curve with parametric equations $x = t^3, y = (1+t)^2$ are:

a) (0,1) b) (-1,0) c) (1,4) d) (-1,4)

La coordonnée du point minimum de la courbe ayant pour équation paramétrique $x = t^3, y = (1+t)^2$ sont:

a) (0,1) b) (-1,0) c) (1,4) d) (-1,4)

6. $\int \frac{5}{1+x^2} dx = \dots$

a) $\frac{-10x}{(1+x^2)^2} + C$ b) $\frac{5}{2x} \ln(1+x^2) + C$

c) $5 \arctan x + C$ d) $5x - \frac{5}{x} + C$

7. If $f(x) = e^{\frac{1}{x}}$, then $f'(x) =$

- a) $\frac{-e^{\frac{1}{x}}}{x^2}$ b) $-e^{\frac{1}{x}}$ c) $\frac{e^{\frac{1}{x}}}{x}$ d) $\frac{e^{\frac{1}{x}-1}}{x}$

Si $f(x) = e^{\frac{1}{x}}$ alors $f'(x) =$

- b) $\frac{-e^{\frac{1}{x}}}{x^2}$ b) $-e^{\frac{1}{x}}$ c) $\frac{e^{\frac{1}{x}}}{x}$ d) $\frac{e^{\frac{1}{x}-1}}{x}$

8. The center of the circle:

$$2x^2 + 2y^2 - 2x + y - \frac{1}{2} = 0 \text{ is:}$$

- a) $(1/2, 1/4)$ b) $(2, -1)$ C) $(-1/2, -1/4)$ d) $(1/2, -1/4)$

Le centre du cercle $2x^2 + 2y^2 - 2x + y - \frac{1}{2} = 0$ est:

- a) $(1/2, 1/4)$ b) $(2, -1)$ C) $(-1/2, -1/4)$ d) $(1/2, -1/4)$

9. Given the differential equation $\cos x \frac{dy}{dx} = y \sin x$, then:

- a) $y = \ln(\sec x) + k$ b) $\ln y = \ln(\sec x) + k$

- , c) $y = \sec x + k$ d) $\ln y = \sec x + k$

Sachant que l'équation différentielle

$$\cos x \frac{dy}{dx} = y \sin x, \text{ Alors :}$$

- b) $y = \ln(\sec x) + k$ b) $\ln y = \ln(\sec x) + k$

- c) $y = \sec x + k$ d) $\ln y = \sec x + k$

10. The range of values of p for which the expression $x^2 + 4px + p$ is:

- a) $p < 0 \text{ or } p > \frac{1}{4}$ b) $p < 0 \text{ and } p > \frac{1}{4}$

- , c) $0 < p < \frac{1}{4}$ d) $0 \leq p \leq \frac{1}{4}$

L'intervalle des valeurs de p pour lesquelles $x^2 + 4px + p$ est:

- b) $p < 0 \text{ or } p > \frac{1}{4}$ b) $p < 0 \text{ and } p > \frac{1}{4}$

- , c) $0 < p < \frac{1}{4}$ d) $0 \leq p \leq \frac{1}{4}$

11. $\int_0^1 \frac{x+1}{x^2+2x-3} dx = \dots$

- a) $-\ln\sqrt{3}$ b) $\frac{-\ln\sqrt{3}}{2}$

- , c) Does not exist d) None of the above

$$\int_0^1 \frac{x+1}{x^2+2x-3} dx = \dots$$

- a) $-\ln\sqrt{3}$ b) $\frac{-\ln\sqrt{3}}{2}$

- b) N'est existe pas d) aucun

12. Let $A = 3\pi r^2 - 4\pi r$. The rate of change of A with respect to r when r = 4 is

- a) 20π b) 32π c) 24π d) 8π

Soit $A = 3\pi r^2 - 4\pi r$. la fréquence de variation de A en fonction de r lorsque r = 4 est

- a) 20π b) 32π c) 24π d) 8π

13. If $e^{\sqrt{3}x} \sin x = R e^{\sqrt{3}x} \sin(x + \alpha)$, then

- a) $R = 1, \alpha = 0$ b) $R = \sqrt{3}, \alpha = 0$

- , c) $R = 1, \alpha = \frac{\pi}{4}$ d) $R = 1, \alpha = \frac{\pi}{2}$

14. Si $e^{\sqrt{3}x} \sin x = R e^{\sqrt{3}x} \sin(x + \alpha)$, alors

- b) $R = 1, \alpha = 0$ b) $R = \sqrt{3}, \alpha = 0$
 ,c) $R = 1, \alpha = \frac{\pi}{4}$ d) $R = 1, \alpha = \frac{\pi}{2}$

15. If $\int_1^2 f(x-c)dx = 5$, where c is a constant, then $\int_{1-c}^{2-c} f(x)dx = \dots\dots\dots$

- a) $5 - c$ b) 5 c) $5 + c$ d) $c - 5$

Si $\int_1^2 f(x-c)dx = 5$, avec c constant, alors $\int_{1-c}^{2-c} f(x)dx = \dots\dots\dots$

- a) $5 - c$ b) 5 c) $5 + c$ d) $c - 5$

16. Given that $y = x^3 e^{x^3}$, then $\frac{dy}{dx} =$

- a) $3x^2 e^{x^3}$ b) $(3x^2 + 3x^5)e^{x^3}$
 ,c) $(3x^2 + x^3)e^{x^3}$ d) $3x^2 e^{x^2}$

Sachant que $y = x^3 e^{x^3}$, alors $\frac{dy}{dx} =$

- a) $5 - c$ b) 5 c) $5 + c$ d) $c - 5$

17. The equation of a line through the origin and perpendicular to $3x - 2y + 4 = 0$ is :

- a) $2x + 3y = 0$ b) $3x - 2y = 0$
 ,c) $9x - 6y - 26 = 0$ d) $3x + 2y = 0$

18. L'équation de la droite passant par l'origine et perpendiculaire à $3x - 2y + 4 = 0$ est :

- b) $2x + 3y = 0$ b) $3x - 2y = 0$
 ,c) $9x - 6y - 26 = 0$ d) $3x + 2y = 0$

19. Given that $\frac{a!}{(a-2)!} = 2$, where a is positive, then the value of a is:

- a) 2 b) 1 c) 4 d) 5

Sachant que $\frac{a!}{(a-2)!} = 2$, avec a positif, alors la valeur de a est :

- a) 2 b) 1 c) 4 d) 5

20. The range of the function $f: x \rightarrow \frac{1+3x}{x}, x \neq 0$ is

- a) $x \in \mathbb{R}, x \neq 3$ b) $x \in \mathbb{R}, x \neq -3$
 ,c) $x \in \mathbb{R}, x \neq \frac{1}{3}$ d) $x \in \mathbb{R}, x \neq \frac{-1}{3}$

L'intervalle de la fonction $f: x \rightarrow \frac{1+3x}{x}, x \neq 0$ is

- b) $x \in \mathbb{R}, x \neq 3$ b) $x \in \mathbb{R}, x \neq -3$
 ,c) $x \in \mathbb{R}, x \neq \frac{1}{3}$ d) $x \in \mathbb{R}, x \neq \frac{-1}{3}$

21. The value(s) of m for which $y = mx - 3$ is tangent to $y = x^2 + 1$ are:

- a) 1 b) ± 2 c) 2