

COMMON ENTRANCE EXAMINATION JULY 2010

SECOND CYCLE TECHNICAL EDUCATION 3HOURS

**PAPER: APPLIED MATHEMATICS (MINOR) FOR ALL ENGINEERING**

**EXERCISE 1: 7 Pts**

Let a function  $ax^2 + bx + c$  periodic function of period  $2\pi$  so that

$$f(0) = f(2\pi) = \pi \text{ and } f(\pi) = 0$$

1. Determine a, b, and c then express  $f(x)$
2. Draw the curve of  $f$  on the interval  $[-4\pi; 4\pi]$
3. Calculate the average value of  $f$  on one period
  - a) determine  $S(f)(x)$  the fourier sum of  $f$
  - b) explain why this sum converges and write the corresponding equality
4. show that the general sum of term  $\frac{(-1)^n}{n^2}$  converges
  - a) determine its sum with the help of the question 3b

**EXERCISE 2: 7 Pts**

Let  $f$  the endomorphism of vectorial space  $E$  basic  $B = (i, j, k)$  defined by  
 $f(i) = j + 2k$ ;  $f(j) = 2j + 4k$  and  $f(k) = 4i + j - 2k$

5. Determine the characteristics polynomial of  $f$
6. Show that the endomorphism  $f$  can be diagonalized and do it
7. Give the passage matrix  $p$  from basic  $B$  to the basic  $B_0$  of eigenvector what formula show the relationship between matrix  $A$  of  $f$  according to basic  $B_0$  ?
8. Compute the reverse matrix  $P^{-1}$

9. Compute the matrix  $D$  [www.touslesconcours.info](http://www.touslesconcours.info)

10. Solve the systems differential equations

$$\begin{cases} \frac{dy}{dt} = 4z \\ \frac{dy}{dt} = x + 2y + z \\ \frac{dz}{dt} = 2x + 4y - 2z \end{cases}$$

**EXERCISE: 36Pts**

One considers the following picture giving the seilling price of  $y$  (in  $10^5$  francs) of a second-hand vehicle according to its  $x$  age (in years)

Age	1	2	3	4	5	6	7	8	
price	2.50	1.70	1.20	1.10	0.90	0.80	0.78	0.40	

One pose  $U = \log(x)$  (  $\log$  means common logarithm ) the calculation will be done from the values approximate to  $10^4$  close to the common logarithms

4. Calculates the linear interrelationship coefficient between  $U$  and  $Y$
5. Determine an equation of the regression right of  $Y$  in  $U$  ( the sense of the root mean square )
6. Give an evaluation of the car price of 10 years age