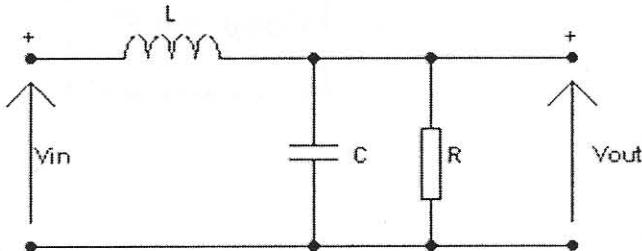


SOLUTION HTTC BAMBILI, ELECTROTECHNICS 2010

EXERCISE 1 :



1.a- Let's find the equivalent impedance viewed from the input

From the figure above, $Z_{eq} = L + C//R$

$$Z_{eq} = jLw + \frac{\frac{R}{jwC}}{R + \frac{1}{jCw}}$$

$$Z_{eq} = jLw + \frac{R}{1 + jwRC}$$

Deducing Z_{eq} in the following cases

i) When w = 2

$$Z_{eq} = j0.4 + \frac{10}{1+j0.8}$$

$$Z_{eq} = 7.57\angle -36.5^\circ (\Omega)$$

Let's deduce the parallel equivalence.

$$Y_p = \frac{1}{R_p} + \frac{1}{X_p}$$

but the series equivalence is given as:

$$Y_s = \frac{1}{7.57\angle -36.3^\circ} = 0.1064 + j0.078$$

$$Y_p = \frac{1}{0.1064} + \frac{1}{j0.078} = 9.4 - j12.82 (\Omega)$$

$$Y_p = 9.4 - j12.82 (si)$$

ii) When w=10

$$Z_{eq} = j10 \times 0.2 + \frac{10}{1+j10 \times 10 \times 0.04}$$

$$Z_{eq} = 0.686\angle -30.98^\circ (\Omega)$$

Deducing the parallel equivalence

$$Y_p = \frac{1}{R_p} + \frac{1}{X_p}; \text{ but } Y_s = \frac{1}{0.686 \angle -30.98^\circ} = 1.458 \angle 30.98^\circ = 1.25 + j0.75$$

$$Y_p = \frac{1}{1.95} + \frac{1}{j0.75} = 0.8 - j1.333; Y_p = 0.8 - j1.333 \text{ (si)}$$

iii) When w=100;

let's deduce the Z_{eq}

$$Z_{eq} = j100 \times 0.2 + \frac{10}{1+j100 \times 10 \times 0.04}; Z_{eq} = 19.75 \angle 89.98^\circ (\Omega)$$

Deducing the parallel equivalence, the series equivalence is given as

$$Y_s = \frac{1}{19.75 \angle 89.98^\circ} = 0.0506 \angle -89.98^\circ = 1.7 \cdot 10^{-5} - j0.0506$$

$$Y_p = \frac{1}{R_p} + \frac{1}{X_p} = \frac{1}{1.7 \cdot 10^{-5}} + \frac{1}{-j0.0506}; Y_p = 56497.18 - j19.76 \text{ (si)}$$

1.b- Let's find the frequency at which Z_{eq} is real.

$$Z_{eq} = jLw + \frac{R}{1+jwRC}$$

$$\begin{aligned} Z_{eq} &= \frac{(jLw(1+jwRC) + R)(1-jwRC)}{1+(wRC)^2} = \frac{(R - LRCw^2 + jLw)(1 - jwRC)}{1 + (wRC)^2} \\ &= \frac{(R - LRCw^2 + LRCw^2 + j(L(RC)^2w^3 - wCR^2 + Lw))}{1 + (wRC)^2} \end{aligned}$$

Z_{eq} is real if $L(RC)^2w^3 - wCR^2 + Lw = 0 \rightarrow w = \sqrt{\frac{CR^2 - L}{L(RC)^2}}$

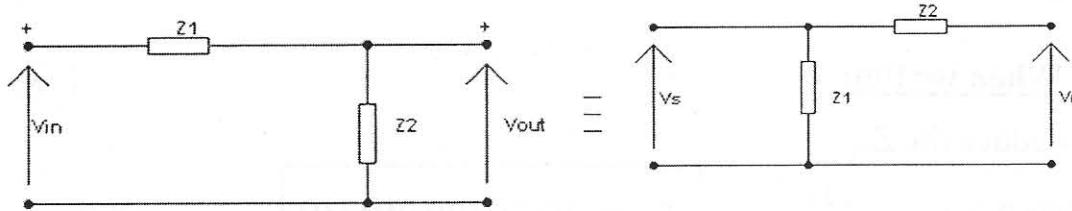
$$f = \frac{\sqrt{CR^2 - L}}{2\pi} ; f = \frac{\sqrt{\frac{0.04 \times 100 - 0.2}{0.2(0.4)^2}}}{2\pi} ;$$

$$f = 1.73 \text{ Hz}$$

1.c Given $V_{in}=100\angle 10^\circ$. Let's determine V_{out}

The circuit becomes

Thevenizing the circuit, it becomes



$$\text{Where } Z_2 = X_C // R \rightarrow Z = \frac{R}{1+j\omega RC}$$

$$\text{Then } V_{out} = \frac{Z_2}{Z_2 + Z_1} V_{in}$$

Note that these values are already calculated above, so let's just deduce Z_2 and Z_1 for the various cases.

i) For $\omega = 2$; $Z_2 = 6.1-j4.878$; $Z_1 = j0.4$

$$Z_2 + Z_1 = 7.57\angle -36.3^\circ (\Omega)$$

$$\text{Then } V_{out} = \frac{7.8\angle -38.65}{7.57\angle -36.3} 100 ;$$

$$V_{out} = 103\angle -2.4^\circ (V)$$

ii) For $\omega = 10$

$$V_{out} = \frac{2.43\angle -75.97}{0.686\angle -30.98} 100 ;$$

$$V_{out} = 354\angle -44.99^\circ (V)$$

iii) $\omega = 100$

$$V_{out} = \frac{0.25\angle -88.57}{19.75\angle 89.98} 100 ;$$

$$V_{out} = 1.266\angle -178.55^\circ (V)$$

EXERCISE 2

Given the following load source configuration

- a) $\Delta - \Delta$; b) $Y-Y$; c) $Y - \Delta$

a) For configuration $\Delta - \Delta$

- *The phase current:*

$$I_L = \sqrt{3}I_p \rightarrow I_p = \frac{I_L}{\sqrt{3}} = \frac{V_1}{Z_1}; Z_1 = R + j(X_L + X_C) = 10\angle 36.87^\circ$$

$$I_p = \frac{V_1}{Z_1} = \frac{220}{10\angle 36.87^\circ};$$

$$I_p = 38.1\angle -36.87^\circ (A)$$

- *Let's calculate the active power*

$$P_a = \sqrt{3}U_L I_L \cos\varphi; P_a = \sqrt{3} \times 220 \times 38.1 \times 0.8;$$

$$P_a = 11.6KW$$

b) For Y-Y connection

$$I_L = I_p \text{ and } U = \sqrt{3}V_p$$

- *The line current:*

$$I_L = I_p = \frac{U}{Z};$$

$$I_L = \frac{\sqrt{3}220}{10\angle 36.87^\circ};$$

$$I_L = 38.1\angle -36.87^\circ (A)$$

- *The absorbed power*

$$P_a = U_L I_L \cos\varphi \text{ but } U_L = \sqrt{3}V_p$$

$$P_a = \sqrt{3} \times 220 \times 38.1 \times 0.8;$$

$$P_a = 11.16KW$$

c) For $Y - \Delta$ connection

$$I_p = \frac{\sqrt{3}V_1}{Z};$$

$$I_p = \frac{\sqrt{3} \times 220 \angle -30^\circ}{10\angle -36.87^\circ};$$

$$I_p = 38.1\angle -6.87^\circ (A)$$

- *Line current*

$$I_L = \sqrt{3} I_p;$$

$$I_L = 66 A$$

- Let's calculate the absorbed power

$$P_a = \sqrt{3} V_1 I_L \cos \varphi ;$$

$$P_a = \sqrt{3} \times 220 \times 66 \times 0.8 ;$$

$$P_a = 34.843 KW$$

2.4 Comparing the Pa consumed in configuration a) and b)

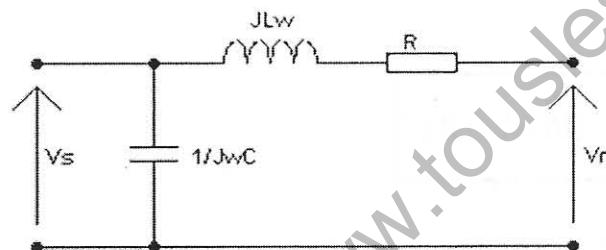
The power consumed in Y is equal to the power consumed in Δ.

2.5 Comparing the power consumed in configuration b) and c)

$$3P_{YY} = P_{Y\Delta}$$

EXERCISE 3

1. Let's draw the electric circuit of this transmission.



a) Sending end voltage

$$V_s = V_r + I_2 Z_2 \quad \text{but } P = V_r I_2 \cos \phi$$

$$\rightarrow I_2 = \frac{P}{V_r \cos \phi}; \quad I_2 = \frac{15000000}{66000 \times 0.8}; \quad I_2 = 284 \angle -36.87^\circ (A)$$

$$V_s = V_r + I_2 Z_2$$

$$V_s = 66000 + 19319.66 + j13897.97;$$

$$V_s = 81097.67 \angle 9.86^\circ (V)$$

b) Sending end current

$$I_s = I_1 + I_2$$

But $I_1 = \frac{V_1}{X_C} = \frac{81097.67 \angle 9.86^\circ}{1714.25 \angle -90^\circ} = 47.3 \angle 99.86^\circ (A)$

$I_s = 47.3 \angle 99.86^\circ + 284 \angle -36.57^\circ ;$

$I_s = 251.66 \angle -29.46^\circ (A)$

c) The sending end power factor

$\cos\phi_S = \cos(9.86 + 29.46) = 39.32^\circ ;$

$P_f = 0.77$

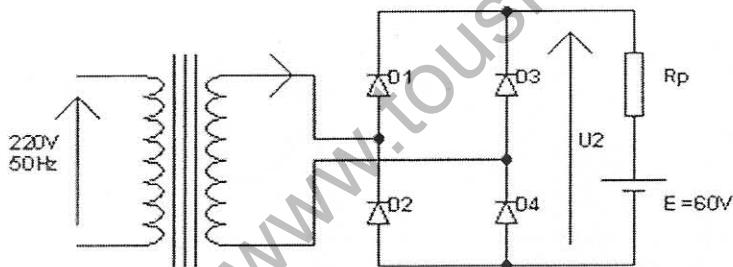
d) The voltage regulation of the line

$V_{reg} = \frac{V_s - V_r}{V_s} \times 100 ;$

$V_{reg} = \frac{81097.67 - 66000}{81097.67} \times 100 ;$

$V_{reg} = 18.6\%$

EXERCISE 4



1- Let's calculate the transformation ratio,

knowing the conducting time is $T/3$

Then $= \frac{2\pi}{3}$; also $z = 2\theta_0 \rightarrow \theta_0 = \frac{\pi}{3}$

$V \cos\theta_0 = E ; V = \frac{E}{\cos\theta_0} = \frac{60}{0.5} ;$

$V = 120V$

Then $m = \frac{V}{V_{in}} = \frac{120}{220} ;$

$m = 0.5455$

2) Calculation of the protective resistance R_p

$$V = E + R_p I \rightarrow R_p = \frac{V - E}{I};$$

$$R_p = \frac{120 - 60}{30} ;$$

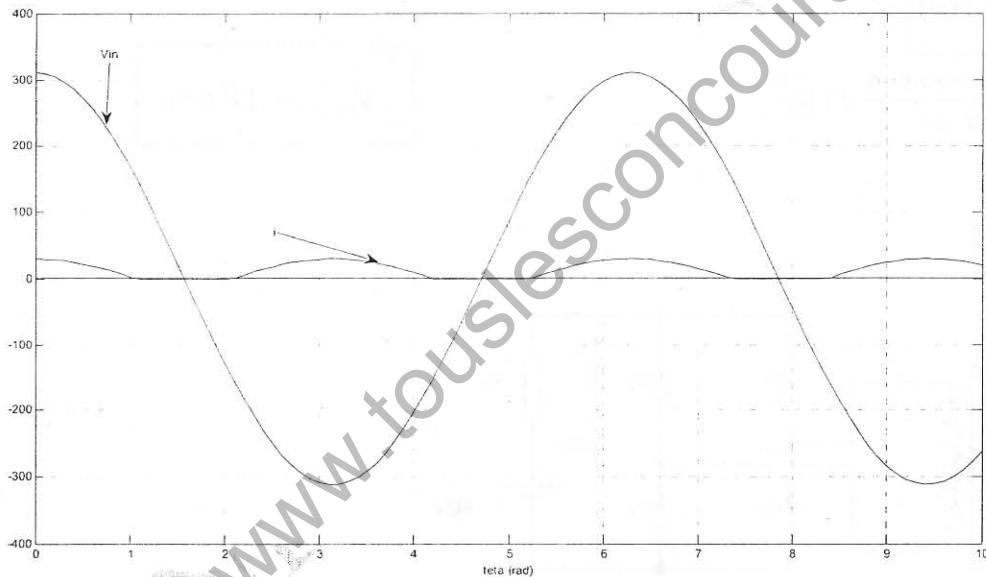
$$R_p = 2\Omega$$

3) Expression of I in function of ϕ where $\phi \in \left[-\frac{\pi}{3}; \frac{\pi}{3}\right]$

The charging current flowing

$$i = \frac{V \cos \phi - E}{R};$$

$$i = 60(\cos \phi - 0.5) \text{ (A)}; \text{ for } \cos \phi > 0; \text{ else } i = 0$$



4) Calculating the average value of i

$$I = \frac{1}{\pi} \int_{\theta_0}^{\theta_1} i d\theta = \frac{1}{\pi} \int_0^{\pi/3} 60(\cos \phi - 0.5) d\phi$$

$$I = 13.1 A$$

5) Calculating the charging time

$$T = Q/I$$

$$= 500/13.1 ;$$

$$T = 38h10min$$

6) Calculating the effective value of i

$$I^2 = \frac{1}{\pi} \int_{\theta_0}^{\theta_1} i^2 d\theta ;$$

$$I^2 = \frac{2}{\pi} \int_0^{\pi/3} 60^2 ((\cos \theta)^2 - \cos \theta + \frac{1}{4}) d\theta ;$$

$$I = 17.65 \text{ A}$$

7) The efficiency of the charger

$$\eta = \frac{P_u}{P_u + P_c} \times 100 ;$$

$$\text{where } P_u = EI = 60 \times 13.1 = 786 \text{ W}$$

$$P_c = R \cdot I^2 = 2 \times 17.65^2 = 623 \text{ W}$$

$$\eta = \frac{786}{786 + 623} \times 100 ;$$

$$\eta = 56\%$$